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# ON THE BLOCK-EDGE TRANSFORMATION GRAPHS $G^{ab}$

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#### ABSTRACT

**I**n this paper, we introduce block-edge transformation graphs. We investigate some basic properties such as connectedness, graph equations and diameters of the block-edge transformation graphs.

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**Keywords:** line graph, jump graph, plick graph, block-edge transformation graphs  $G^{ab}$ .

### 1. INTRODUCTION

All the graphs considered here are finite, undirected without loops or multiple edges. We refer to [4] for unexplained terminology and notation. A *block* of a graph is connected nontrivial graph having no cutvertices. Let G = (V, E) be a graph with block set  $U(G) = \{B_i; B_i \text{ is a block of } G\}$ . If a block  $B \in U(G)$  with the edge set  $\{e_1, e_2, \ldots, e_r; r \geq 1\}$ , then we say that the edge  $e_i$  and block B are incident with each other, where  $1 \leq i \leq r$ . The block B and an edge e are said to be adjacent if e is adjacent with at least one incident edge of B, otherwise not adjacent. The *line graph* L(G) of a graph G is the graph with vertex set as the edge set of G and two vertices of G are adjacent whenever the corresponding edges in G have a vertex in common. The *jump graph* G is the graph whose the vertex set is the edge set of G and two vertices of G are not adjacent in G. The *plick graph* G is the graph G is the graph whose set of vertices is the union of the set of edges and blocks of G and in which two vertices are adjacent if and only if the corresponding edges of G are adjacent or one is corresponds to an edge and other is corresponds to a block are incident. This concept is introduced by G is the graph of a graph, we define the following block-edge transformation graphs.

**Definition:** Let G = (V, E) be a graph with a block set  $U(G) = \{B_i; B_i \text{ is a block of } G\}$ , and a, b be two variables taking values + or -. The block-edge transformation graph  $G^{ab}$  is a graph whose vertex set is  $E(G) \cup U(G)$ , and two vertices x and y of  $G^{ab}$  are joined by an edge if and only if one of the following holds:

- (i) Suppose x and y are in E(G). a = + if x, y are adjacent in G; a = if x and y are not adjacent in G.
- (ii) Suppose  $x \in E(G)$  and  $y \in U(G)$ . b = + if x, y are incident with each other in G; b = if x, y are not incident with each other in G.

Thus, we obtain four kinds of block-edge transformation graphs  $G^{++}$ ,  $G^{+-}$ ,  $G^{-+}$  and  $G^{--}$  in which  $G^{++}$  is exactly the plick graph of G. Some other graph valued functions were studied in [1, 5, 8, 9, 11]. The vertex  $e_i^{'}$  ( $B_i^{'}$ ) of  $G^{ab}$  corresponding to edge  $e_i$  (block  $B_i$ ) of  $G^{ab}$  and is referred as edge (block)-vertex.

The following will be useful in the proof of our results.

**Remark: 1.1** L(G) is an induced subgraph of  $G^{++}$  and  $G^{+-}$ .

**Remark: 1.2** I(G) is an induced subgraph of  $G^{-+}$  and  $G^{--}$ .

**Theorem: 1.1 [4]** If G is connected, then L(G) is connected.

**Theorem: 1.2 [12]** Let G be a graph of size  $q \ge 1$ . Then J(G) is connected if and only if G contains no edge that is adjacent to every other edge of G unless  $G = K_4$  or  $C_4$ .

If a disconnected graph G has no isolated vertices, then clearly G contains no edge that is adjacent to every other edge of G. By Theorem 1.2, we have the following remark.

**Remark: 1.3** If a disconnected graph G has no isolated vertices, then J(G) is connected.

Since block-edge transformation graphs  $G^{ab}$  are defined on the edge set and block set of a graph G, isolated vertices of G (if G has) play no rule in  $G^{ab}$ . We assume that the graph G under consideration is nonempty and has no isolated vertices. In this paper, We investigate some basic properties of these four kinds of block-edge transformation graphs.

## 2. CONNECTEDNESS OF $G^{ab}$

The first theorem is well-known.

**Theorem: 2.1** For a given graph G,  $G^{++}$  is connected if and only if G is connected.

**Theorem: 2.2** For a given graph G,  $G^{+-}$  is connected if and only if  $G \neq B_i \cup B_j$  is not a block, where  $B_i$  and  $B_j$  are blocks.

**Proof:** Suppose  $G \neq B_i \cup B_i$  is not a block. Then we consider the following cases:

**Case-1.** Suppose G is connected. Then it has at least two blocks. Hence by Theorem 1.1 and Remark 1.1, L(G) is a connected subgraph of  $G^{+-}$ , and also each block-vertex  $B_i^{'}$  in  $G^{+-}$  is adjacent to at least one edge-vertex  $e_j^{'}$ , where  $e_j$  is not incident with  $B_i$  in G. Thus  $G^{+-}$  is connected.

Case-2. Suppose G is disconnected. Then it has at least three blocks. We see that in  $G^{+-}$ , each block-vertex  $B_i^{'}$  is adjacent to at least two edge-vertices  $e_j^{'}$ , where  $e_j^{'}$  is not incident with  $B_i^{'}$  in G, and each edge-vertex  $e_j^{'}$  is adjacent to edge-vertex  $e_k^{'}$  and at least two block-vertices  $B_i^{'}$  in  $G^{+-}$ , where  $e_k^{'}$  is adjacent to  $e_j^{'}$ , and  $B_i^{'}$  is not incident with  $e_j^{'}$  in G. Since in such a case, there is a path between any two vertices of  $G^{+-}$ . Hence  $G^{+-}$  is connected.

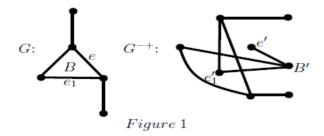
Conversely, suppose  $G^{+-}$  is connected. If G is a block, then  $G^{+-} = L(G) \cup K_1$  is disconnected, a contradiction. If  $G = B_i \cup B_j$ , then  $G^{+-}$  is a disconnected graph having two components namely  $L(B_i) + K_1$  and  $L(B_j) + K_1$ , a contradiction.

**Theorem: 2.3** For a given graph G,  $G^{-+}$  is connected if and only if G contains no block  $K_2$  that is adjacent to every other edge of G.

**Proof:** Suppose a graph G contains no block  $K_2$  that is adjacent to every other edge of G. If G is a block, then  $G^{-+} = J(G) + K_1$  is connected. If G has more than one block, then we consider the following two cases:

**Case-1.** If G contains no edge that is adjacent to every other edge of G, then by Remark 1.2 and Theorem 1.2, J(G) is a connected subgraph of  $G^{-+}$ , and in  $G^{-+}$ , each block-vertex  $B_i^{'}$  is adjacent to at least one edge-vertex  $e_j^{'}$ , where  $e_j$  is incident with  $B_i$  in G. Thus  $G^{-+}$  is connected.

**Case-2.** If G contains an edge e that is adjacent to every other edge of G, then clearly e is incident with a block B of size more than 2. And  $(G - e)^{-+}$  is a connected subgraph of  $G^{-+}$  and  $e', B', e'_1$  is a path in  $G^{-+}$  (see fig. 1), where  $e_1$  is incident with B, and each block-vertex  $B'_i$  in  $G^{-+}$  is adjacent to at least one edge-vertex  $e'_j$ , where  $e_j$  is incident with  $B_i$  in G. Hence  $G^{-+}$  is connected.



Conversely, suppose  $G^{-+}$  is connected. Assume G contains a block  $K_2$ , say e, that is adjacent to every other edge of G, then it is easy to see that  $G^{-+}=(G-e)^{-+}\cup K_2$  is disconnected, a contradiction.

**Theorem: 2.4** For a given graph G,  $G^{--}$  is connected if and only if  $G \neq P_3$  is not a block.

**Proof:** Suppose  $G \neq P_3$  is not a block. We consider the following two cases:

**Case-1.** Suppose G contains no edge that is adjacent to every other edge of G. Then by Remark 1.2 and Theorem 1.2, J(G) is a connected subgraph of  $G^{--}$ , and each block-vertex  $B_i'$  is adjacent to at least one edge-vertex  $e_j'$  in  $G^{--}$ , where  $e_i$  is not incident with  $B_i$  in G. Thus  $G^{--}$  is connected.

Case-2. Suppose G contains an edge e that is adjacent to all other edge of G. Then by definition of  $G^{--}$ , each edge-vertex  $e'_i$  is adjacent to edge-vertex  $e'_i$  and at least one block-vertex  $B'_j$ , where  $B_j$  is not incident with  $e_i$ , and  $e_k$  is not adjacent to  $e_i$  in G. And also each block-vertex  $B'_j$  is adjacent to at least one edge-vertex  $e'_i$ , where  $e_i$  is not incident with  $B_j$  in G. Hence there is a path between any two vertices of  $G^{--}$ . Therefore  $G^{--}$  is connected.

Conversely, suppose  $G^{--}$  is connected. If G is a block, then  $G^{--} = J(G) \cup K_1$  is disconnected, a contradiction. If  $G = P_3$ , then  $G^{--} = 2K_2$  is disconnected, a contradiction.

## 3. GRAPH EQUATIONS AND ITERATIONS OF $G^{ab}$

For a given graph operator  $\Phi$ , which graph is fixed under  $\Phi$ ?, that is  $\Phi(G) = G$ . It is well known in [10] that for a given graph G, the interchange graph G' = G if and only if G is a 2-regular graph.

For a given block-edge transformation graph  $G^{ab}$ , we define the iteration of  $G^{ab}$  as follows:

1.  $G^{(ab)^1} = G^{ab}$ 

2.  $G^{(ab)^n} = [G^{(ab)^{n-1}}]^{ab}$  for  $n \ge 2$ .

The isomorphism of G and  $G^{++}$  are shown in [6].

**Theorem: 3.1** The graphs G and  $G^{+-}$  are isomorphic if and only if  $G = 2K_2$ .

**Proof:** Suppose  $G^{+-} = G$ . Assume  $G \neq 2K_2$ . We consider following two cases:

**Case-1.** Suppose G is a block. Then clearly  $G^{+-} = L(G) \cup K_1$  is disconnected. Thus  $G^{+-} \neq G$ , a contradiction.

Case-2. Suppose G has at least two blocks with q edges. Then  $G^{+-}$  has at least 2q-1 edges. Hence the number of edges in G is less than that in  $G^{+-}$ . Thus  $G^{+-} \neq G$ , a contradiction.

Conversely, suppose  $G = 2K_2$ . Then it is easy to see that  $G^{+-} = G$ .

**Corollary: 3.2** The graphs G and  $G^{(+-)^n}$  are isomorphic if and only if  $G = 2K_2$ .

**Theorem: 3.3** The graphs G and  $G^{-+}$  are isomorphic if and only if  $G = K_2$ .

**Proof:** Suppose  $G^{-+} = G$ . Assume  $G \neq K_2$  with  $p \geq 3$  vertices. We consider the following two cases:

**Case-1.** Suppose G is connected. We consider the following two subcases:

**Subcase-1.1.** Suppose G is a tree with p vertices. Then G has p-1 edges and p-1 blocks. Thus  $G^{-+}$  has 2p-2 vertices. Hence the number of vertices of G is less than that in  $G^{-+}$ . Therefore  $G^{-+} \neq G$ , a contradiction.

**Subcase-1.2.** Suppose G is not a tree with p vertices. Then G has at least p edges and at least one block. Thus  $G^{-+}$  has at least p+1 vertices. Hence  $G^{-+} \neq G$ , a contradiction.

Case-2. Suppose G is a disconnected graph with q edges. Then  $G^{-+}$  has at least q+1 edges. Hence  $G^{-+} \neq G$ , a contradiction.

Conversely, suppose  $G = K_2$ . Then clearly  $G^{-+} = G$ .

**Corollary: 3.4** The graphs G and  $G^{(-+)^n}$  are isomorphic if and only if  $G = K_2$ .

**Theorem: 3.5** For any graph G,  $G^{--} \neq G$ .

**Proof:** If  $G = K_2$ , then  $G^{--} = 2K_1 \neq G$ . We consider the following two cases:

**Case-1.** Suppose  $G \neq K_2$  is a connected graph. Since the definitions of  $G^{-+}$  and  $G^{--}$ , we have  $|V(G^{-+})| = |V(G^{--})|$ . By proof of the Theorem 3.3, we have  $|V(G)| \neq |V(G^{-+})|$ . Hence  $|V(G)| \neq |V(G^{--})|$ . Therefore  $G^{--} \neq G$ .

**Case-2.** Suppose G is a disconnected graph with q edges. Then  $G^{--}$  has at least q+1 edges. Hence  $|E(G)| \neq |E(G^{--})|$ . Therefore  $G^{--} \neq G$ . From all the above two cases, we have  $G^{--} = G$ .

**Corollary: 3.6** For any graph G,  $G^{(--)^n} \neq G$ .

## 4. DIAMETERS OF Gab

The distance between two vertices  $v_i$  and  $v_j$ , denoted by  $d(v_i, v_j)$ , is the length of the shortest path between the vertices  $v_i$  and  $v_j$  in G. The shortest  $v_i - v_j$  path is often called *geodesic*. The *diameter* of a connected graph G, denoted by diam(G), is the length of any longest geodesic.

In this section, we consider the diameters of  $G^{ab}$ .

**Theorem: 4.1** If G is a connected graph, then  $diam(G^{++}) \leq diam(G) + 1$ .

**Proof:** Let G be a connected graph. We consider the following three cases:

Case-1. Assume G is a tree. Then it is easy to see that  $diam(G^{++}) = diam(G) + 1$ .

Case-2. Assume G is a cycle  $C_n$  for  $n \ge 3$ . Then  $G^{++} = W_{n+1}$  and  $diam(G^{++}) < diam(G) + 1$ .

**Case-3.** Assume G contains a cycle  $C_n$  for  $n \ge 3$ . Corresponding to cycle  $C_n$ ,  $W_{n+1}$  appears as subgraph in  $G^{++}$ . Therefore  $diam(G^{++}) \le diam(G) + 1$ .

From all the above three cases, we have  $diam(G^{++}) \leq diam(G) + 1$ .

**Theorem: 4.2** If a graph G has at least three blocks, then  $diam(G^{+-}) = \begin{cases} 2 \text{ if every component of } G \text{ has at least one cutvertex} \\ 3 \text{ if at least one component of } G \text{ is a block.} \end{cases}$ 

**Proof:** Let  $e'_1$ ,  $e'_2$  be the two edge-vertices of  $G^{+-}$ . If  $e_1$  and  $e_2$  are adjacent edges in G, then  $e'_1$  and  $e'_2$  are adjacent in  $G^{+-}$ . If  $e_1$  and  $e_2$  are not adjacent edges in G, then there exists a block G which is incident with neither G in G such that G is a path of length 2 in G in G then there exists a block G which is incident with neither G in G such that G is a path of length 2 in G in G then there exists a block G which is incident with neither G in G such that G is a path of length 2 in G in G then there exists a block G which is incident with neither G is a path of length 2.

Let  $B_1'$ ,  $B_2'$  be the two block-vertices of  $G^{+-}$ . Then there exists an edge e which is incident with neither  $B_1$  nor  $B_2$  in G such that  $B_1'$ , e',  $B_2'$  is a path in  $G^{+-}$  of length 2.

Let e' and B' be the edge-vertex and block-vertex of  $G^{+-}$  respectively. If e is not incident with B in G, then e' and B' are adjacent in  $G^{+-}$ . If e is incident with B in G, then we consider the following two cases:

**Case-1.** If every component of G has at least one cutvertex, then there exists an edge  $e_1$  which is adjacent to e, and is not incident with B such that e',  $e'_1$ , B' is a path of length 2 in  $G^{+-}$ .

**Case-2.** If at least one component of G is a block, say B, then there exists not incident block  $B_1$  and edge  $e_1$ , where  $B_1$  is not incident with e, and  $e_1$  is incident with neither B nor  $B_1$  such that e',  $B'_1$ ,  $e'_1$ , B' is a path in  $G^{+-}$  of length 3.

**Theorem: 4.3** If a connected graph G has two blocks, then  $diam(G^{+-}) \leq 5$ .

**Proof:** Suppose G is a connected graph with two blocks  $B_1$  and  $B_2$  of size  $q_1$  and  $q_2$  respectively. Then  $K_{1,q_1}$  and  $K_{1,q_2}$  are two edge-disjoint subgraphs of  $G^{+-}$ . And there exists at least one edge e' in  $G^{+-}$  is incident with exactly one pendant vertex of  $K_{1,q_1}$  and  $K_{1,q_2}$ . It is easy that see that the diameter of star is at most 2.

Hence  $diam(G^{+-}) = diam(K_{1,q_1}) + diam(K_{1,q_2}) + 1 \le 2 + 2 + 1 = 5$ .

**Theorem:** 4.4 If a graph G contains no block  $K_2$  that is adjacent to other edge of G, then  $daim(G^{-+}) \leq 5$ .

**Proof:** For  $e'_1$ ,  $e'_2$  be the two edge-vertices of  $G^{-+}$ . If  $e_1$  and  $e_2$  are not adjacent edges in G, then  $e'_1$  and  $e'_2$  are adjacent in  $G^{-+}$ . If  $e_1$  and  $e_2$  are adjacent edges in G, then we have one of the following case:

**Case-1.** If  $e_1$  and  $e_2$  are incident with same block B, then  $e'_1$ ,  $B'_1$ ,  $e'_2$  is a path of length 2 in  $G^{-+}$ .

Case-2. If  $e_1$  and  $e_2$  are incident with different blocks  $B_1$  and  $B_2$  respectively, then we have the following subcases:

**Subcase-2.1.** If there is an edge e which is adjacent to neither  $e_1$  nor  $e_2$  in G, then  $e_1'$ ,  $e_2'$  is a path in  $G^{-+}$  of length 2.

**Subcase-2.2.** If there is an edge e which is incident with  $B_2$ , and is not adjacent to  $e_1$ , then  $e'_1, e'_1, e'_2, e'_2$  is a path in  $G^{-+}$  of length 3.

**Subcase-2.3.** If there are two not adjacent edges  $e_3$  and  $e_4$ , where  $e_3$  and  $e_4$  are not adjacent to  $e_1$  and  $e_2$  respectively, then  $e'_1, e'_3, e'_4, e'_2$  is a path in  $G^{-+}$  of length 3.

For  $B_1'$ ,  $B_2'$  be the two block-vertices of  $G^{-+}$ . Let  $e_1$  and  $e_2$  be the two edges incident with the blocks  $B_1$  and  $B_2$  respectively. We have the following cases:

**Case-1.** If  $e_1$  and  $e_2$  are not adjacent edges in G, then  $B'_1, e'_1, e'_2, B'_2$  is a path of length 3 in  $G^{-+}$ .

**Case-2.** If  $e_1$  and  $e_2$  are adjacent edges in G, then we have the following subcases:

**Subcase-2.1.** If there is an edge e which is adjacent to neither  $e_1$  nor  $e_2$  in G, then  $B'_1, e'_1, e'_2, B'_2$  is a path of length 4 in  $G^{-+}$ .

**Subcase-2.2.** If there are two not adjacent edges  $e_3$  and  $e_4$ , where  $e_3$  and  $e_4$  are not adjacent to  $e_2$  and  $e_1$  respectively, then  $B_1'$ ,  $e_1'$ ,  $e_2'$ ,  $e_3'$ ,  $e_2'$ ,  $B_2'$  is a path in  $G^{-+}$  of length 5.

For  $e_1'$  and  $B_2'$  be the edge-vertex and block-vertex of  $G^{-+}$  respectively. If  $e_1$  is incident with  $B_2$  in G, then  $e_1'$  and  $B_2'$  are adjacent in  $G^{-+}$ . If  $e_1$  is not incident with  $B_2$  in G, then we have the following cases:

Case-1. If there is an edge  $e_2$  is incident with  $B_2$ , where  $e_2$  is not adjacent to  $e_1$  in G, then  $B_2', e_2', e_1'$  is a path in  $G^{-+}$  of length 2.

**Case-2.** If there is an edge  $e_2$  is incident with  $B_2$ , and is adjacent to an edge e in G, where  $e_1$  and e are incident with  $B_1$ , then  $B_2', e_2', e_1', B_1', e_1'$  is a path of length 4 in  $G^{-+}$ .

**Case-3.** If there is an edge e which is adjacent to neither  $e_1$  nor  $e_2$ , and  $e_2$  is incident with  $B_2$ , then  $B_2'$ ,  $e_2'$ ,  $e_2'$ ,  $e_1'$  is a path of length 3 in  $G^{-+}$ .

**Theorem: 4.5** If a graph  $G \neq P_3$  is not a block, then  $diam(G^{--}) \leq 4$ .

**Proof:** Let  $e'_1$ ,  $e'_2$  be the two edge-vertices of  $G^{--}$ . If  $e_1$  and  $e_2$  are not adjacent edges in G, then  $e'_1$  and  $e'_2$  are adjacent in  $G^{--}$ . If  $e_1$  and  $e_2$  are adjacent edges in G, then we have one of the following case:

Case-1. If  $e_1$  and  $e_2$  are incident with same block, then there exist a block B which is incident with neither  $e_1$  nor  $e_2$  such that  $e_1'$ , B',  $e_2'$  is a path of length 2 in  $G^{--}$ .

Case-2. If  $e_1$  and  $e_2$  are incident with different blocks  $B_1$  and  $B_2$  respectively in G, then we have the following subcases:

**Subcase-2.1.** If there is a block B which is incident to neither  $e_1$  nor  $e_2$  in G, then  $e_1'$ , B',  $e_2'$  is a path in  $G^{--}$  of length 2.

**Subcase-2.2.** If there is an edge e is incident with block  $B_2$ , and is not adjacent to  $e_1$ , then  $e'_2$ ,  $B'_1$ , e',  $e'_1$  is a path in  $G^{--}$  of length 3.

**Subcase-2.3.** If there is an edge  $e_3$  which is adjacent to neither  $e_1$  nor  $e_2$ , then  $e_1'$ ,  $e_3'$ ,  $e_2'$  is a path in  $G^{--}$  of length 2.

Let  $B_1'$ ,  $B_2'$  be two block-vertices of  $G^{--}$ . We have the following cases:

Case-1. If there is an edge e which is incident with neither  $B_1$  nor  $B_2$ , then  $B_1'$ , e',  $B_2'$  is a path of length 2 in  $G^{--}$ .

**Case-2.** If there are two not adjacent edges  $e_1$  and  $e_2$  are incident with  $B_1$  and  $B_2$  respectively, then  $B_1', e_2', e_1', B_2'$  is a path of length 3 in  $G^{--}$ .

Let e' and B' be the edge-vertex and block-vertex of  $G^{--}$  respectively. If e is not incident with B in G, then e' and B' are adjacent in  $G^{--}$ . If e is incident with B in G, then we have the following cases:

**Case-1.** If there is an edge  $e_1$  is incident with B, and is not adjacent to edge e in G, then e',  $e'_1$ , B' is a path in  $G^{--}$  of length 2.

**Case-2.** If there are two not adjacent edges  $e_1$  and  $e_2$ , where  $e_1$  is not incident with B, and  $e_2$  is not adjacent to e, then  $B', e'_1, e'_2, e'$  is a path of length 3 in  $G^{--}$ .

**Case-3.** If there are not incident edge  $e_2$  and block  $B_3$ , where  $e_2$  is not incident with B, and  $B_3$  is not incident to e, then e',  $B'_3$ ,  $e'_2$ , B' is a path of length 3 in  $G^{--}$ .

**Case-4.** If there is an edge  $e_1$  which is incident with  $B_1$ , and is not adjacent to an edge  $e_2$ , where  $e_2$  is incident with B, then  $B', e'_1, e'_2, B'_1, e'$  is a path of length 4 in  $G^{--}$ .

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